

Two-magnon Raman scattering from the  $\text{Cu}_3\text{O}_4$  layers in  $(\text{Sr}_2, \text{Ba}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$ Joakim Holmlund,<sup>1</sup> Christopher S. Knee,<sup>1,4</sup> Jakob Andreasson,<sup>1,5</sup> Mats Granath,<sup>2</sup> A. P. Litvinchuk,<sup>3</sup> and Lars Börjesson<sup>1</sup><sup>1</sup>Department of Applied Physics, Chalmers University of Technology, SE-412 96 Göteborg, Sweden<sup>2</sup>Department of Physics, University of Gothenburg, SE-412 96 Göteborg, Sweden<sup>3</sup>Department of Physics and Texas Center for Superconductivity, University of Houston, Texas 77204, USA<sup>4</sup>Department of Chemistry, University of Gothenburg, SE-412 96 Göteborg, Sweden<sup>5</sup>Department of Cell and Molecular Biology, Uppsala University, SE-751 24 Uppsala, Sweden

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$(\text{Sr}_2, \text{Ba}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$  are antiferromagnetic insulators which are akin to the parent compounds of the cuprate superconductors but with two distinct magnetic ordering temperatures related to two magnetic  $\text{Cu}_\text{I}$  and  $\text{Cu}_\text{II}$  spin sublattices. Here we present a study of these materials by means of Raman spectroscopy. Following the temperature and polarization dependence of the data, we readily identify two distinct features at around 3000 and 300  $\text{cm}^{-1}$  that are related to two-magnon scattering from the two sublattices. The estimated spin-exchange coupling constants for the  $\text{Cu}_\text{I}$  and  $\text{Cu}_\text{II}$  sublattices are found to be  $J_\text{I} \sim 139\text{--}143(132\text{--}136)$  meV and  $J_\text{II} \sim 14(11)$  meV for Sr(Ba) compounds. Moreover, we observe modes at around 480 and 445  $\text{cm}^{-1}$  for the Sr and Ba containing samples, respectively, which disappears at the ordering temperature of the  $\text{Cu}_\text{II}$ . We argue that these modes may also be of magnetic origin and possibly related to interband transitions between the  $\text{Cu}_\text{I}\text{--}\text{Cu}_\text{II}$  sublattices.

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## I. INTRODUCTION

The enormous effort of trying to understand the origin of high-temperature superconductivity (HTS) in the cuprate superconductors during the past decades has led to the exploration of many new avenues regarding the field of strongly correlated electrons. It is clear that the copper oxide plane substructures, which are common to all these materials, are an essential ingredient. A defining feature of the superconducting (SC) planes is their magnetism, and the undoped planes are well described as square lattice quantum Heisenberg antiferromagnets (SLQHA). It is generally believed that the magnetism has a close connection to the HTS.<sup>1–3</sup> Therefore the study of the SLQHA, as well as its generalizations, is an important problem. The oxychloride 2342 phases  $(\text{Ba}_2, \text{Sr}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$  resemble the HTS insulating parent compounds but with an additional twist of having two intercalated SLQHA (Fig. 1). The crystal structure remains tetragonal in the interval  $15 < T < 550$  K.<sup>4</sup> The key feature of the structure is the presence of  $\text{Cu}_3\text{O}_4$  planes, consisting of a  $\text{Cu}_\text{I}$  sublattice, which is isostructural to that of the ordinary  $\text{CuO}_2$  planes, combined with an interpenetrating  $\text{Cu}_\text{II}$  sublattice. The antiferromagnetic (AFM) ordering of the  $\text{Cu}_\text{I}$  and  $\text{Cu}_\text{II}$  spins upon lowering the temperature was first observed from magnetic-susceptibility and electron-paramagnetic-resonance measurements;<sup>5,6</sup> the results indicated Néel temperatures are  $T_\text{NI} \sim 386(332)$  K and  $T_\text{NII} \sim 40(31)$  K for  $\text{Sr}_2(\text{Ba}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$ , respectively. The results are in line with expectations in which the vanishing mean field from the  $\text{Cu}_\text{I}$  spins cause an independent ordering of the  $\text{Cu}_\text{II}$  spins but with a preferred collinearity due to quantum spin-wave interactions.<sup>7</sup>

From related cuprates such as  $\text{YBa}_2\text{Cu}_3\text{O}_{6.1}$  and  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$ , it has been shown that the magnetic exchange coupling in the  $\text{Cu}_\text{I}$  SLQHA have values of approximately  $J \sim 130$  meV.<sup>8,9</sup> For the 2342 phases there are two more

couplings to consider: we have the ordering of the second sublattice and its exchange coupling  $J_\text{II}$ , and also the interaction between the two magnetic lattices  $J_\text{I–II}$  [see Fig. 1(b)]. The  $J_\text{I–II}$  coupling is expected to be ferromagnetic by the Kanamori-Goodenough-Anderson rule due to the Cu–O–Cu  $90^\circ$  bond; however, because of the vanishing mean field for antiferromagnetically ordered  $\text{Cu}_\text{I}$ , it only comes into play through fluctuations. Magnetization measurements,<sup>4,10</sup> and comprehensive elastic, quasielastic, and inelastic neutron-

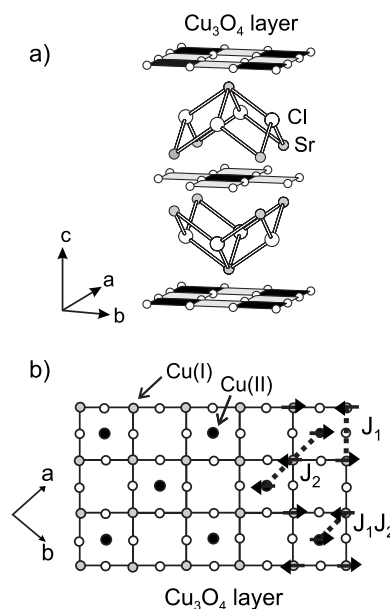


FIG. 1. (a) Crystal structure of  $(\text{Sr}_2, \text{Ba}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$ ; in the  $\text{Cu}_3\text{O}_4$  sheets shaded square planes have a central  $\text{Cu}(\text{I})$  ion, black square planes have central  $\text{Cu}(\text{II})$  ions, and small open spheres are oxygen. (b)  $\text{Cu}_3\text{O}_4$  plane with exchange interactions between spins indicated. Ordered spin directions for copper spins are shown as arrows.

scattering experiments<sup>9,11</sup> show that the copper lattices display differing ordering criticalities with the Cu<sub>II</sub> lattice exhibiting a two-dimensional (2D) Ising dependence. Kim and co-workers<sup>9,11</sup> also report evidence of coupling between Cu<sub>I</sub> and Cu<sub>II</sub> as the Cu<sub>I</sub> out-of-plane gap increases below  $T_{MI}$ , and state that the  $J_{II}$  and  $J_{I-II}$  couplings should be of similar size, around 10 meV. In contradiction to the experimentally determined values of  $J_{I-II}$  coupling from Kim and co-workers,<sup>9,11</sup> Yaresko *et al.*<sup>12</sup> calculated the exchange integrals of Ba<sub>2</sub>Cu<sub>3</sub>O<sub>4</sub>Cl<sub>2</sub> through a local-density approximation (LDA) including on-site correlations (LDA+ $U$ ) method and reported higher values of the  $J_{I-II} \sim 20$  meV. They also report slightly lower values of the  $J_{II}$  coupling.

When it comes to the fluctuations in this system that drive the order-from-disorder phase transitions, the thermal and quantum fluctuations do not compete. However, introducing chemical disorder in the system will cause quenched random exchange fields that will compete with quantum fluctuations and give rise to new interesting perspectives. Recent neutron-scattering measurements by Ramazanoglu *et al.*<sup>6</sup> indicate spin-glass formation between the two magnetic phase transitions in Co substituted Ba<sub>2</sub>Cu<sub>2.95</sub>Co<sub>0.05</sub>O<sub>4</sub>Cl<sub>2</sub>. Magnetization data also shows a strong ferromagnetic enhancement upon Co substitution.

In this study we investigate the two interpenetrating magnetic sublattices using Raman-scattering (RS) spectroscopy. For the ordinary HTS materials the interaction of light with the spin degrees of freedom<sup>13</sup> gives a two-magnon (2M) peak in the Raman spectra of a frequency shift  $\omega$  near 2.8 J in the  $B_{1g}$  scattering geometry for a tetragonal  $D_{4h}$  symmetry.<sup>8,14</sup> The main objective of the present study is to identify two-magnon peaks associated with the Cu<sub>I</sub> and Cu<sub>II</sub> sublattice ordering, and determine the magnitude of the corresponding exchange interactions. Because of the extended unit cell (containing in the plane one Cu<sub>II</sub> and two Cu<sub>I</sub> ions plus oxygen), the lattice vectors are rotated by 45° with the Cu<sub>I</sub> mode expected in the  $B_{2g}$  and  $A_{1g}+B_{2g}$  geometry, and the Cu<sub>II</sub> mode in  $B_{1g}$  and  $A_{1g}+B_{1g}$  geometry. We do indeed find two features with the expected polarization dependence at a shift of around 3000 and 300 cm<sup>-1</sup>, respectively. The one at low energy appears around the lower Néel temperature as expected for magnons of the Cu<sub>II</sub> antiferromagnetic order. In addition we find an unexpected feature with a nontrivial temperature dependence around 480 cm<sup>-1</sup> that we tentatively assign to have a magnetic origin most likely related to Cu<sub>I</sub>-Cu<sub>II</sub> particle-hole excitations decaying through a Cu<sub>I</sub> two-magnon process. The Raman signature, if any, of Cu<sub>I</sub>-Cu<sub>II</sub> excitations for intermediate temperatures  $T_{II} < T < T_I$  is a challenging open problem which is complicated by the fact that the Cu<sub>II</sub> spins are paramagnetic (in fact very weakly ferromagnetic<sup>4</sup>) and so cannot be treated in mean-field theory as for the Cu<sub>I</sub>.<sup>15,16</sup>

## II. EXPERIMENTAL

Small crystallites of Sr<sub>2</sub>Cu<sub>3</sub>O<sub>4</sub>Cl<sub>2</sub> were obtained by slow cooling (2.0 °C/h) a partial melt of Sr<sub>2</sub>Cu<sub>3</sub>O<sub>4</sub>Cl<sub>2</sub> powder from 1005 °C. For Ba<sub>2</sub>Cu<sub>3</sub>O<sub>4</sub>Cl<sub>2</sub> the melt was cooled from a lower temperature of 965 °C. The Raman measurements

were performed in back-scattering geometry using a DILOR-XY800 spectrometer/Raman microscope equipped with notch filters and operated in the single grating mode. The spectral resolution was  $\sim 2$  cm<sup>-1</sup> and the diameter of the probed area was  $\sim 2$  μm. An Ar<sup>+</sup>/Kr<sup>+</sup> laser was used for excitation with a laser power at the sample kept at 1 mW to avoid laser heating. The wavelength used was 514.5 (2.4 eV). The crystals were probed in different scattering geometries. To denote the scattering geometries in our Raman experiments, we use the Porto notation, i.e.,  $d_1(p_1p_2)d_2$ . Here  $d_1$  and  $d_2$  are the direction of the incoming and detected light, respectively, and  $p_1$  and  $p_2$  are the polarization of the incoming and detected light, respectively. The Porto labels are to be taken along the crystal axes, i.e.,  $x=a$  axis,  $y=b$  axis, and  $z=c$  axis. For a  $D_{4h}$  group the Raman-active representations are  $A_{1g}$ ,  $B_{1g}$ ,  $B_{2g}$ , and  $E_g$  only while  $A_{2g}$  is silent. The specific scattering configurations presented here were  $z(x'y')\bar{z}$ ,  $z(xy)\bar{z}$ ,  $z(x'x')\bar{z}$ ,  $z(yy)\bar{z}$ , and  $z(xx)\bar{z}$  which correspond to  $B_{1g}$ ,  $B_{2g}$ ,  $A_{1g}+B_{2g}$ ,  $A_{1g}+B_{1g}$ , and  $A_{1g}+B_{1g}$  Raman-active representations, respectively. Variable temperature measurements were performed using a cold-finger LHe cryostat equipped with a heater, and Raman intensity calibration was done using a BaF crystal as a standard. All extracted information (such as positions, intensities, and shifts) from the peaks comes from applying Gaussian fits to the two-magnon peaks and Lorentzian fits to the phonons, and then compensating for the respective Bose occupation factor involved.

## III. RESULTS

The Raman scattering from our samples will be covered in three different subsections for Sr<sub>2</sub>Cu<sub>3</sub>O<sub>4</sub>Cl<sub>2</sub>. First we will discuss the region around 3000 cm<sup>-1</sup> where we observe a strong two-magnon peak, followed by the range around 300 cm<sup>-1</sup> where we observe another two-magnon excitation. Finally, we will discuss the phonon spectra and a feature, at around 480 cm<sup>-1</sup>. We also present data from measurements of Ba<sub>2</sub>Cu<sub>3</sub>O<sub>4</sub>Cl<sub>2</sub> as a comparison.

### A. Two-magnon peak at around 3000 cm<sup>-1</sup>

This feature has a strong polarization selection rule dependence. Figure 2 shows that it is predominant in  $z(xy)\bar{z}$ ,  $z(x'x')\bar{z}$ , and  $z(y'y')\bar{z}$  scattering configurations. It is very weak or absent in  $z(xx)\bar{z}$  and  $z(x'y')\bar{z}$  scattering configurations. Moreover the perfectly overlapping  $z(x'x')\bar{z}$  and  $z(y'y')\bar{z}$  scattering configurations reflect the isotropic  $xy$  plane. This polarization dependence indicates that the feature is a two-magnon peak of the Cu<sub>I</sub> sublattice. In Fig. 3 we present a temperature-dependent study that shows how the peak hardens continuously from around 3130–3230 cm<sup>-1</sup> from room temperature (RT) to 8 K. Both the asymmetric shape of the feature, together with the excitation energy, further strongly support the assignment of the peak to a two-magnon excitation from the Cu<sub>I</sub> magnetic superstructure seen before in similar compounds with square Cu-O lattice.<sup>8,14</sup>

### B. Two-magnon peak at around 300 cm<sup>-1</sup>

Figure 4 shows the temperature dependence of the low energy region up to 1600 cm<sup>-1</sup>; the figure shows the behav-

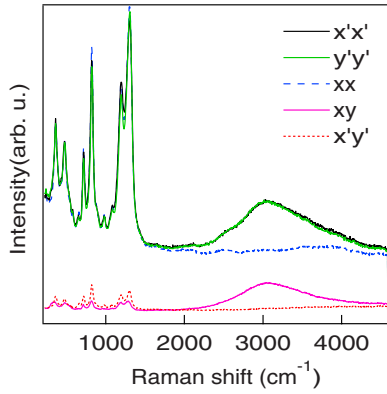


FIG. 2. (Color online) Raman spectra for  $\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in  $z(x'y')\bar{z}$ ,  $z(x'x)\bar{z}$ ,  $z(xx)\bar{z}$ ,  $z(xy)\bar{z}$ , and  $z(y'y')\bar{z}$  scattering configurations. The spectra are collected with an excitation wavelength of 514.5 nm at RT.

ior of the phonons and magnetic interactions in the structure in  $z(x'y')\bar{z}$  scattering configuration.

In order to separate the features we mark the peaks 1–6 which corresponds to energies of  $\sim 180$ , 310 (two-magnon), 360, 480, 543, and 660  $\text{cm}^{-1}$ , respectively. Most interesting are peaks 2 and 4, which emerge and disappear at low temperatures, respectively. The behavior of the feature at around

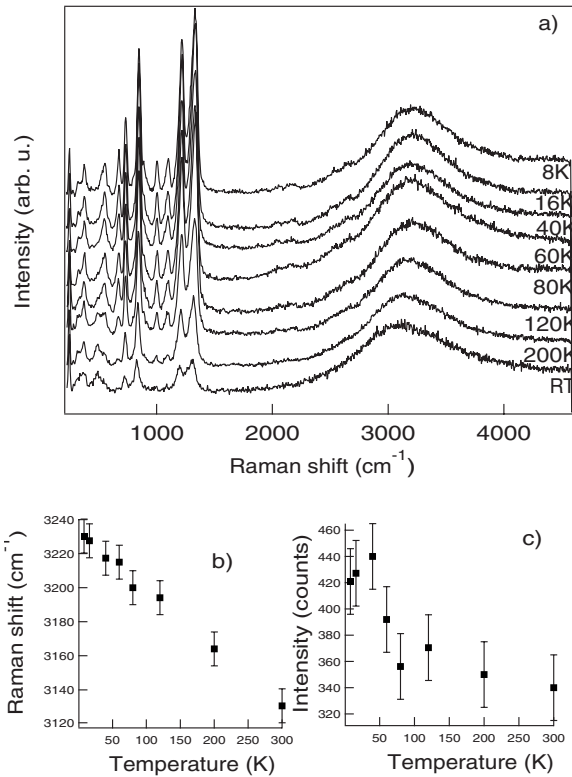


FIG. 3. (a) Temperature-dependent Raman spectra for  $\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in  $z(xy)\bar{z}$  scattering configuration for excitation wavelength of 514.5 nm from RT down to 8 K. The graphs are shown with a vertical offset in order to separate the spectra. (b) and (c) show the position and integrated intensity of the  $\sim 3000 \text{ cm}^{-1}$  peak plotted against the temperature, respectively. The spectra are Bose compensated.

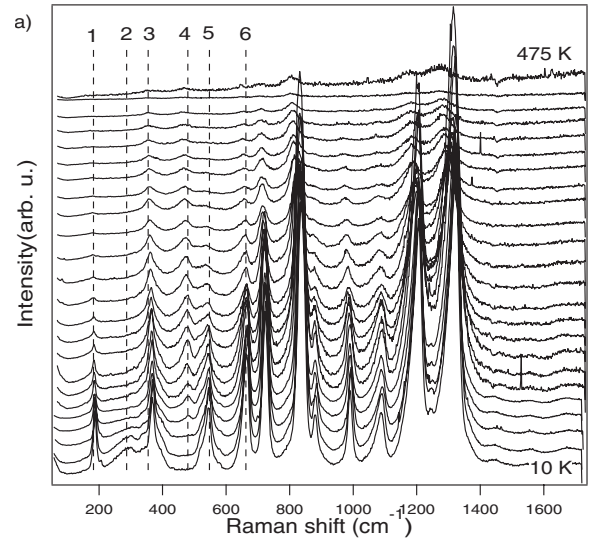


FIG. 4. (a) Temperature-dependent Raman spectra for  $\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in  $z(x'y')\bar{z}$  scattering configuration for excitation wavelength of 514.5 nm from 300 down to 10 K. The peaks numbered 1–6 correspond to energies of  $\sim 180$ , 310 (2-magnon), 360, 480, 543, and 660  $\text{cm}^{-1}$ , respectively (the spectra taken at 475 K is scaled by a factor of 3). (b) The integrated intensities of the  $\sim 310$  and  $\sim 480 \text{ cm}^{-1}$  modes together with a dotted curve based on a 2D Ising model  $(T_N - T)^\beta$ , where  $T_N = 40 \text{ K}$  is the Néel temperature determined from Ref. 5 and  $\beta = 0.125$ . All spectra are Bose compensated.

300  $\text{cm}^{-1}$ , labeled peak 2, shows that the peak emerges at low temperatures: first appearing between 80 and 60 K, and then the intensity grows rapidly down to 20 K before it saturates at a position  $\sim 310 \text{ cm}^{-1}$  [inset of Fig. 4; the inset includes a dotted curve based on a 2D Ising model  $(T_N - T)^\beta$ , where  $T_N = 40 \text{ K}$ ]. In contrast to the 3000  $\text{cm}^{-1}$  peak this peak is seen in  $z(x'y')\bar{z}$  scattering configuration, where the former was seen in  $z(xy)\bar{z}$  scattering configuration. Both its temperature and polarization dependence indicate that this feature arises from  $\text{Cu}_{\text{II}}$  two-magnon scattering.

### C. Phonon spectra including the feature at around 480 $\text{cm}^{-1}$

The phonon Raman spectra of  $\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  is complicated in many ways. It has a number of phonons that do not follow normal Bose-Einstein occupation statistics; instead there are several phonons, including higher order phonons that grow anomalously with decreased temperature (see Figs. 3 and 4). This has earlier been reported for compounds in-

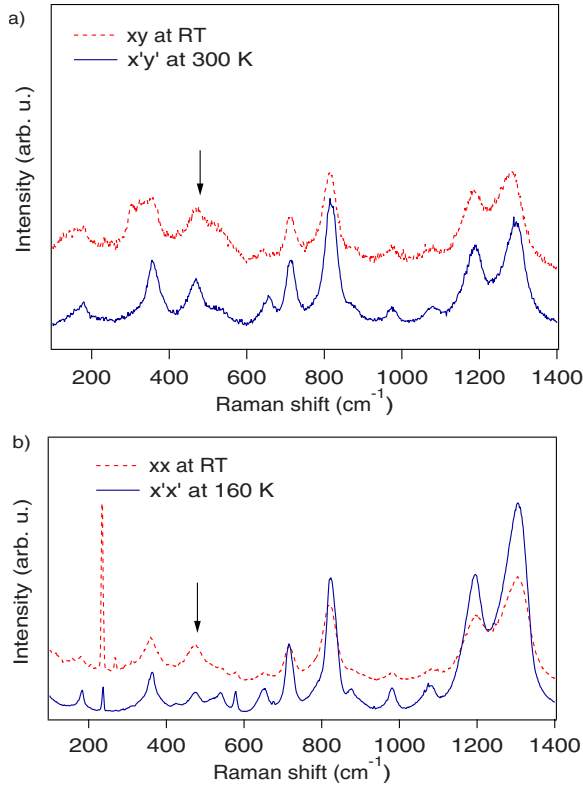


FIG. 5. (Color online) Raman spectra for  $\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in (a)  $z(x'y')\bar{z}$  and  $z(xy)\bar{z}$ , and (b)  $z(x'y')\bar{z}$  and  $z(xx)\bar{z}$  scattering configurations. The spectra are collected with an excitation wavelength of 514.5 nm at RT, 300 K, and 160 K. The 480  $\text{cm}^{-1}$  peak is marked in the figures.

cluding spin chains and has been explained by Fröhlich interaction induced activation of longitudinal phonons.<sup>17–19</sup> These effects have only been seen when the incoming and scattered light has been polarized along the chains and ladders. However, in  $(\text{Sr}_2, \text{Ba}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$  we observe this extreme behavior in cross-polarized scattering configuration (see Figs. 3 and 4). In  $z(x'y')\bar{z}$  (Fig. 4) and  $z(xy)\bar{z}$  (Fig. 3) scattering configurations, we observe a peak at around 480  $\text{cm}^{-1}$  with different and even more peculiar temperature dependence. The peak can be seen in all measured scattering configurations [ $z(xy)\bar{z}$ ,  $z(x'y')\bar{z}$ ,  $z(xx)\bar{z}$ , and  $z(x'x')\bar{z}$ ] (see Fig. 5). Furthermore, the peak loses intensity upon lowering the temperature from 475 K and it approaches zero at a finite temperature at around 60 K. Since the crystal structure is stable in this interval, a possible explanation would be that its origin is a two-phonon difference mode. At first sight there are two modes at around 660 (peak 6) and 180  $\text{cm}^{-1}$  (peak 1) that appear to match the difference criterion as shown in Fig. 6. Here we plot the temperature dependence of the shifts for all three modes (180, 480, and 660  $\text{cm}^{-1}$ ) together with the difference between the 180 and 660  $\text{cm}^{-1}$  phonon modes. The difference condition starts to break down above 200 K and the gap increases at higher temperatures, displaying a clear mismatch at 475 K. Hence the difference mode explanation is not likely. Instead, given the modes sensitivity to the ordering of the  $\text{Cu}_{\text{II}}$  spins, it seems more likely that the mode has a magnetic origin and, if so, is probably

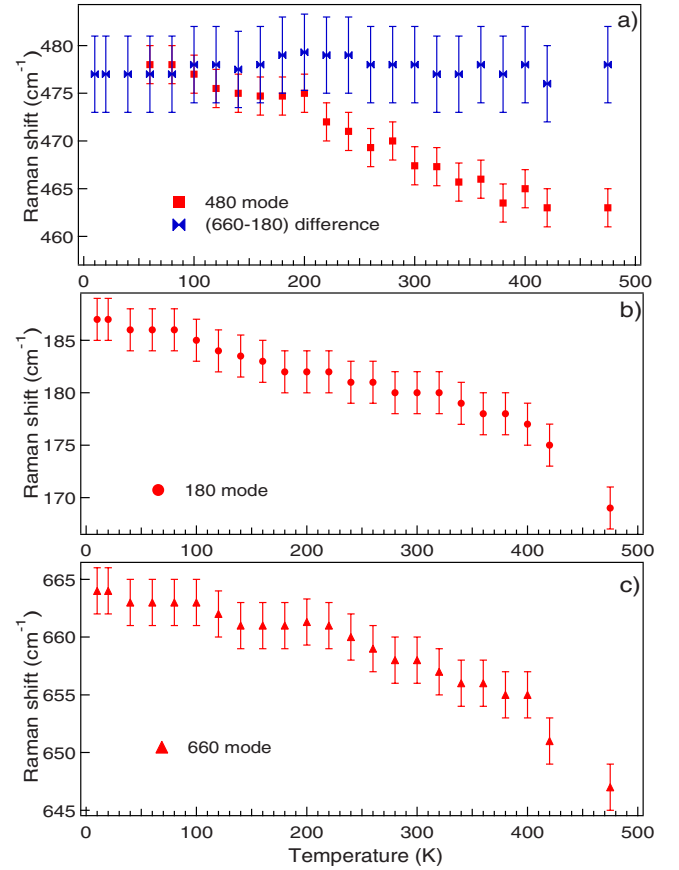


FIG. 6. (Color online) Temperature dependence of the Raman shifts for the (a) 480, (b) 180, and (c) 660  $\text{cm}^{-1}$  phonon modes in  $z(x'y')\bar{z}$  scattering configuration for excitation wavelength of 514.5 nm from 475 down to 10 K. The information is extracted from applying Lorentzian fits of the three phonon modes. In addition (a) shows the difference of the 660 and 180  $\text{cm}^{-1}$  modes with increasing temperature.

related to the  $\text{Cu}_{\text{I}}$  magnon which is the only expected coherent magnetic mode at these temperatures. The energy shift from the  $\text{Cu}_{\text{I}}$  two-magnon decay may be due to the  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{II}}$  energy difference.

#### D. $\text{Ba}_2\text{Cu}_3\text{O}_4\text{Cl}_2$

For comparison we made similar Raman measurements on a compound where Ba was substituted for Sr (see Fig. 7). All spectra showed a similar behavior in the Raman-scattering data as for the  $\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  compound, with the exception of somewhat different energies for the excitations upon switching to Ba. Figure 7(a) displays the temperature dependence for the  $\sim 3000$   $\text{cm}^{-1}$  peak. The peak hardens from around 2990  $\text{cm}^{-1}$  and grows in intensity down to the second Néel temperature at around 30 K, and then it remains at approximately 3080  $\text{cm}^{-1}$  and shows a weak drop in intensity. Figure 7(b) displays the temperature dependence for the  $\sim 300$   $\text{cm}^{-1}$  peak. The peak is more prominent than in the Sr-substituted compound and the position at 10 K is at  $\sim 237$   $\text{cm}^{-1}$ , compared with 310  $\text{cm}^{-1}$  for the former. Figure 8 displays the low energy region in four different scattering



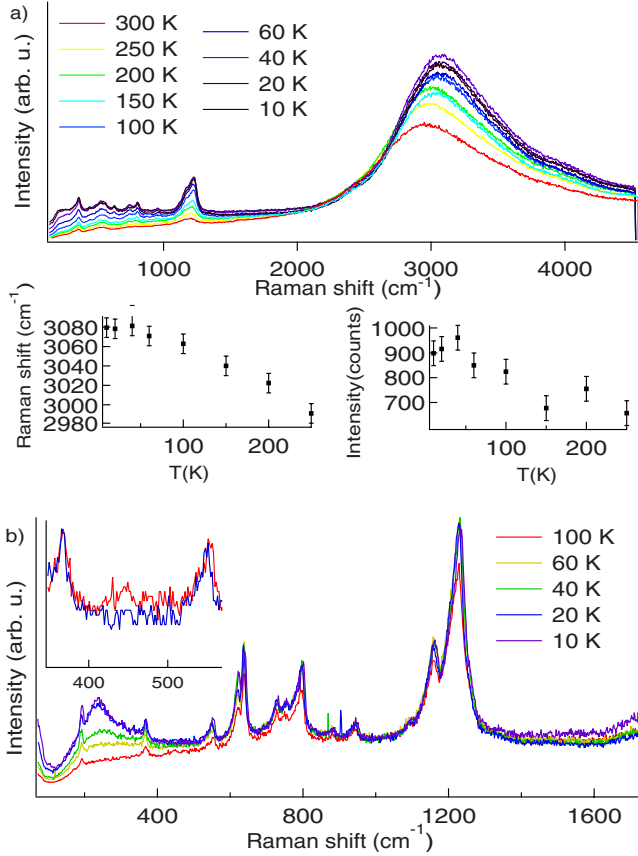


FIG. 7. (Color online) (a) Temperature-dependent Raman spectra for  $\text{Ba}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in  $z(xy)\bar{z}$  scattering configuration. The left and the right insets show the position and integrated intensity of the  $\sim 3000 \text{ cm}^{-1}$  peak plotted against the temperature, respectively. (b) Raman spectra for  $\text{Ba}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in  $z(x'y')\bar{z}$  scattering configuration for excitation wavelength of 514.5 nm from 300 to 10 K. The small inset shows a zoom up of the  $\sim 445 \text{ cm}^{-1}$  mode. The spectra are Bose compensated.

configurations with light polarized along  $xx$ ,  $xy$ ,  $x'x'$ , and  $x'y'$ . From the figure one can clearly observe the peak at  $\sim 230 \text{ cm}^{-1}$  in  $x'y'$  and  $xx$ . This is easily compared with the  $\text{Cu}_{\text{II}}$  magnetic sublattice seen in Fig. 1(b). The selection rules

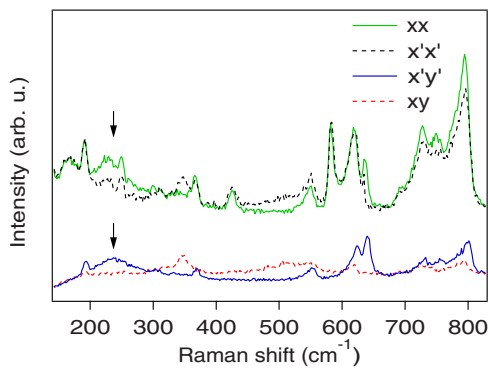


FIG. 8. (Color online) Raman spectra for  $\text{Ba}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  in  $z(xy)\bar{z}$ ,  $z(x'y')\bar{z}$ ,  $z(xx)\bar{z}$ , and  $z(x'x')\bar{z}$  scattering configurations. The spectra are collected with an excitation wavelength of 514.5 nm at 10 K. The  $\sim 230 \text{ cm}^{-1}$  peak is marked in the figures.

TABLE I. Peak positions and superexchange coupling constants. Magnon peak = 2.8 J.

Compound	$\text{Sr}_2\text{Cu}_3\text{O}_4\text{Cl}_2$	$\text{Ba}_2\text{Cu}_3\text{O}_4\text{Cl}_2$
$\text{Cu}_{\text{I}} (\text{cm}^{-1})$	3130–3230	2990–3080
$J_{\text{I}} (\text{meV})$	139–143	132–136
$T (\text{K})$	300–8	300–10
$\text{Cu}_{\text{II}} (\text{cm}^{-1})$	$\sim 310$	$\sim 240$
$J_{\text{II}} (\text{meV})$	13.7	10.6
$T (\text{K})$	10	10

apply well if one considers that the  $\text{Cu}_{\text{II}}$  magnetic superstructure is rotated by  $45^\circ$  with respect to the  $\text{Cu}_{\text{I}}$  magnetic superstructure. The shift to lower energy for the two-magnon peaks in the Ba substituted compound compared to the Sr-substituted compound would also be in accordance with the expected weaker superexchange due to increased  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{I}}$  and  $\text{Cu}_{\text{II}}\text{-Cu}_{\text{II}}$  separations. In addition we observed the corresponding  $\text{Cu}_{\text{I-II}}$  magnetic mode for this compound, the position at 100 K is at  $\sim 445 \text{ cm}^{-1}$  [see inset of Fig. 7(b)].

#### IV. DISCUSSION

The results clearly distinguish several interesting features in the Raman spectra, of which at least two most probably stem from magnetic scattering. This assertion is strengthened as the 2342 phases exhibit no structural transitions upon decreasing temperature.<sup>4</sup> The most prominent feature is the broad and intense peak at  $\sim 3000 \text{ cm}^{-1}$ . The energy of the feature is similar to other SLQHA system with a  $J \sim 130 \text{ meV}$  (Ref. 8) and the selection rules apply well for a typical two-magnon excitation from the  $\text{Cu}_{\text{I}}$  magnetic sublattice. Table I reveals a slight shift to lower energies for the peak maxima in  $\text{Ba}_2\text{Cu}_3\text{O}_4\text{Cl}_2$  reflecting the increased  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{I}}$  separation and weakened superexchange in this compound, i.e., the  $a$  parameters for the Sr and Ba analogs are 5.462 and 5.517 Å, respectively.

The next feature to consider is the peak that emerges at around the second Néel temperature  $\sim 31$  and 40 K for Ba and Sr compounds, respectively.<sup>5,6</sup> The selection rules for this feature clearly shows a relation to the  $\text{Cu}_{\text{II}}$  magnetic superstructure considering a  $45^\circ$  rotation of the magnetic superstructure with respect to the  $\text{Cu}_{\text{I}}$  lattice. The energy of the peak also allows the  $J_{\text{II}}$  coupling to be estimated and, as shown in Table I, the derived values agree pretty well with measured  $J$ -coupling constants from neutron-scattering experiments  $J \sim 10 \text{ meV}$ .<sup>9,11</sup> The redshift observed for the Ba compound also fits the expected trend. One further point concerns the apparently non-2D-Ising growth of the feature shown in the inset of Fig. 4. This discrepancy most likely reflects the different length scales probed by the Raman and diffraction techniques. In fact, our data show that the two magnon first appears in the 60 K data, significantly above the  $T_{\text{NII}}$  of Kim *et al.*,<sup>9</sup> emphasizing that a long-range interplanar correlation is not required for the short-wavelength spin waves probed by our light-scattering experiment.<sup>20</sup>

The peak at around  $480 \text{ cm}^{-1}$  displays an unusual non-monotonic temperature dependence. The simplest explanation

tion for this feature would be that it is a two-phonon difference mode. However the behavior upon increasing the temperature appears to rule out this explanation. The intensity of the peak decreases toward lower temperatures and it completely disappears below  $T \approx 60$  K (Fig. 4). This temperature coincides very well with the growth of the  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{II}}$  two magnon, which reflects the ordering of the second magnetic lattice. The peak could thus be severely affected by the  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{II}}$  ordering which points toward a magnetic origin. The present Raman experiments are done in the resonant regime in which the current operator creates particle-hole excitations across the Mott-Hubbard gap. Excitations both within the sublattices as well as between sublattices are expected, and the energy difference  $3000\text{-}480 \approx 2500$   $\text{cm}^{-1}$  (300 meV) would then reflect the  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{II}}$  site energy difference, which is in fact roughly in line with a LDA estimate of 380 meV.<sup>21</sup> As mentioned in Sec. I this is a particularly difficult problem in the intermediate temperature regime where the  $\text{Cu}_{\text{II}}$  spins are not ordered. Whether any additional coherent magnetic response apart from the ordinary  $\text{Cu}_{\text{I}}$  two magnon should be expected is an open problem.

Finally, we discuss briefly the profile shape of the two-magnon peaks. The  $\sim 3000$   $\text{cm}^{-1}$  magnon has a typical high energy tail seen in other similar SLQHA systems (see, for example, Blumberg *et al.*<sup>8</sup>). In contrast the 300  $\text{cm}^{-1}$  two magnon appears to have a low energy tail. Theoretical work has been relatively successful in predicting the shape and polarization dependence of the usual ( $\text{Cu}_{\text{I}}$ ) two magnon (see, for example, Ref. 22, and references therein) for layered cuprate antiferromagnets. However at this stage it is difficult to comment further concerning the profile since there are at least two phonons that screen the high energy side, making it difficult to reliably deconvolute the two-magnon scattering.

Furthermore, for the Ba substituted compound, the notch filter cuts the low energy side and thus prevents us from analyzing the two-magnon profile at lower energies in a satisfactory way. It is hoped that these data presented here on the 2342 systems will provide a basis for extension of the theories for quantum antiferromagnets.

## V. SUMMARY

In summary we have studied the magnetic scattering in  $(\text{Sr}_2, \text{Ba}_2)\text{Cu}_3\text{O}_4\text{Cl}_2$  through the sensitive probe of magnetic Raman scattering. Based on the temperature dependence and selection rules, we assign the peaks at  $\sim 3000$  and  $\sim 300$   $\text{cm}^{-1}$  to two-magnon excitation peaks stemming from the  $\text{Cu}_{\text{I}}$  and  $\text{Cu}_{\text{II}}$  sublattices, respectively. From the peak positions, we have obtained estimates of the strength of the  $J$  couplings for the  $\text{Cu}_{\text{I}}\text{-Cu}_{\text{I}}$  and  $\text{Cu}_{\text{II}}\text{-Cu}_{\text{II}}$  interactions of around 140 and 14 meV, respectively. In addition an interesting mode is observed at  $\sim 480$   $\text{cm}^{-1}$ , which most probably has a magnetic origin related to the coupling between the  $\text{Cu}_{\text{I}}$  and  $\text{Cu}_{\text{II}}$  sublattices. Further work regarding an extension of existing theories for resonant magnetic Raman response is needed to describe the intermediate ( $T_{\text{MI}} < T < T_{\text{MII}}$ ) temperature range of these materials. In addition, investigations with applied magnetic fields could be of high interest in order to resolve unanswered questions regarding the magnetic interactions in these materials.

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